# Demo: Networks from Real Data 

## Networks from real data

First off, what directory are we in?
In[0]:= Directory[]
Out[0]= /Users/gigglepuss
I have a data file!

I really really like League of Legends. It's an online competitive video game. The game developers have their own "restful" API (RESTful is just a standardized API) for collecting any amount of data on the video game... for free! But you do need to make an account to get the data. Check it out here: https://developer.riotgames.com/
Anyways, I downloaded data from the API through Python and then transformed the data into a network. I saved the network into a JSON file.

Here's how I structured the network: Character A ---> Character B Means that A won a game against B. The weight means the number of games where $A$ beat $B$. This network has parallel edges that go in opposite directions, meaning edges $A-->B$ and $B-->A$ can both exist, each with their own edge weight. There are $140+$ nodes in this network and one full month worth of games for 200 players in North America (only the best 200 players on the server!).

I only collected the data and made a network, I know nothing about it!

Let's see if we can load the file here:
$\ln [2]:=$ json = Import["PycharmProjects/League/network_demo.json"]

$$
\begin{aligned}
&\{\text { directed } \rightarrow \text { True, multigraph } \rightarrow \text { False, graph } \rightarrow \ldots 1 \cdots, \text { nodes } \rightarrow\{\cdots 1 \cdots, \text { links } \rightarrow \\
&\{\text { weight } \rightarrow 42, \text { source } \rightarrow 81, \text { target } \rightarrow 53\},\{\text { weight } \rightarrow 92, \text { source } \rightarrow 81, \text { target } \rightarrow 43\}, \\
&\{\text { weight } \rightarrow 148, \text { source } \rightarrow 81, \text { target } \rightarrow 164\},\{\text { weight } \rightarrow 203, \\
&\text { source } \rightarrow 81, \text { target } \rightarrow 145\},\{\text { weight } \rightarrow 28, \text { source } \rightarrow 81, \text { target } \rightarrow 240\}, \\
&\text { \{weight } \rightarrow 38, \text { source } \rightarrow 81, \text { target } \rightarrow 99\},\{\text { weight } \rightarrow 48, \text { source } \rightarrow 81, \text { target } \rightarrow 62\}, \\
&\{\text { weight } \rightarrow 491, \text { source } \rightarrow 81, \text { target } \rightarrow 236\},\{\text { weight } \rightarrow 52, \text { source } \rightarrow 81, \\
&\text { target } \rightarrow 432\},\{\text { weight } \rightarrow 207, \text { source } \rightarrow 81, \text { target } \rightarrow 555\}, \\
&\{\text { weight } \rightarrow 67, \text { source } \rightarrow 81, \text { target } \rightarrow 238\},\{\text { weight } \rightarrow 56, \text { source } \rightarrow 81, \text { target } \rightarrow 28\}, \\
&\{\text { weight } \rightarrow 112, \text { source } \rightarrow 81, \text { target } \rightarrow 202\}, \ldots 18216 \ldots, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 5\},\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 163\}, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 89\},\{\text { weight } \rightarrow 2, \text { source } \rightarrow 75, \text { target } \rightarrow 53\}, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 238\},\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 55\}, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 427\},\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 114\}, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 30\},\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 58\}, \\
&\{\text { weight } \rightarrow 2, \text { source } \rightarrow 75, \text { target } \rightarrow 497\},\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 51\}, \\
&\{\text { weight } \rightarrow 1, \text { source } \rightarrow 75, \text { target } \rightarrow 105\}\}\}
\end{aligned}
$$

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Hm... We need to get this into a format Mathematica will like!

## If you're a data engineer, this is what you do! ;)

Let's look at the Graph function to see what kinds of formats it accepts.
Graph
It would be easiest to made an edge list like with the CAs above. We can put the weights in there as well, as long as we preserve the order of the edges.
It looks like we can get all of this information from the "links ->" part of the file.
links = Lookup[json, "links"]

```
\(\{\) \{weight \(\rightarrow 42\), source \(\rightarrow 81\), target \(\rightarrow 53\}\),
    \{weight \(\rightarrow 92\), source \(\rightarrow 81\), target \(\rightarrow 43\}\), \(\{\) weight \(\rightarrow 148\), source \(\rightarrow 81\), target \(\rightarrow 164\}\),
    \{weight \(\rightarrow 203\), source \(\rightarrow 81\), target \(\rightarrow 145\}\),
    \(\{\) weight \(\rightarrow 28\), source \(\rightarrow 81\), target \(\rightarrow 240\}\), \(\{\) weight \(\rightarrow 38\), source \(\rightarrow 81\), target \(\rightarrow 99\}\),
    \(\{\) weight \(\rightarrow 48\), source \(\rightarrow 81\), target \(\rightarrow 62\}, \ldots 18229 \ldots\),
    \(\{\) weight \(\rightarrow 1\), source \(\rightarrow 75\), target \(\rightarrow 114\}\), \(\{\) weight \(\rightarrow 1\), source \(\rightarrow 75\), target \(\rightarrow 30\}\),
    \(\{\) weight \(\rightarrow 1\), source \(\rightarrow 75\), target \(\rightarrow 58\}\), \{weight \(\rightarrow 2\), source \(\rightarrow 75\), target \(\rightarrow 497\}\),
    \(\{\) weight \(\rightarrow 1\), source \(\rightarrow 75\), target \(\rightarrow 51\}\), \(\{\) weight \(\rightarrow 1\), source \(\rightarrow 75\), target \(\rightarrow 105\}\}\)
```

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Let's get rid of those arrows.

$$
\begin{aligned}
& \{\{42,81,53\},\{92,81,43\},\{148,81,164\},\{203,81,145\},\{28,81,240\}, \\
& \{38,81,99\},\{48,81,62\},\{491,81,236\},\{52,81,432\},\{207,81,555\}, \\
& \{67,81,238\},\{56,81,28\},\{112,81,202\},\{76,81,516\},\{129,81,8\}, \\
& \{139,81,104\},\{46,81,31\},\{66,81,114\},\{66,81,41\},\{82,81,64\}, \\
& \{76,81,201\},\{41,81,51\},\{32,81,1\},\{43,81,96\}, \ldots 18194 \cdots, \\
& \{2,75,25\},\{2,75,142\},\{2,75,80\},\{3,75,145\},\{1,75,54\},\{1,75,20\}, \\
& \{2,75,98\},\{1,75,1\},\{1,75,91\},\{1,75,85\},\{1,75,21\},\{1,75,5\}, \\
& \{1,75,163\},\{1,75,89\},\{2,75,53\},\{1,75,238\},\{1,75,55\},\{1,75,427\}, \\
& \{1,75,114\},\{1,75,30\},\{1,75,58\},\{2,75,497\},\{1,75,51\},\{1,75,105\}\}
\end{aligned}
$$

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That is a nice list! It is a list of lists. For each of the lists in the list, we can make an edge list by taking the second and third element. How can we easily take them? By making a special function! But this time we are going to do it in shorthand. In this format, the \# is the variable, the \& activates it, and /@ means "apply it to all the elements in this list".
$\ln [5]:=$ edges $=\#[[2]] \rightarrow \#[[3]] \& / @$ links

$$
\begin{aligned}
\{81 & \rightarrow 53,81 \rightarrow 43,81 \rightarrow 164,81 \rightarrow 145,81 \rightarrow 240,81 \rightarrow 99,81 \rightarrow 62,81 \rightarrow 236,81 \rightarrow 432, \\
81 & \rightarrow 555,81 \rightarrow 238,81 \rightarrow 28,81 \rightarrow 202,81 \rightarrow 516,81 \rightarrow 8,81 \rightarrow 104,81 \rightarrow 31, \\
81 & \rightarrow 114,81 \rightarrow 41,81 \rightarrow 64,81 \rightarrow 201,81 \rightarrow 51,81 \rightarrow 1,81 \rightarrow 96,81 \rightarrow 79,81 \rightarrow 83, \\
81 & \rightarrow 98,81 \rightarrow 13,81 \rightarrow 40,81 \rightarrow 107,81 \rightarrow 85,81 \rightarrow 203,81 \rightarrow 58,81 \rightarrow 245, \\
81 & \rightarrow 5,81 \rightarrow 35,81 \rightarrow 26,81 \rightarrow 136,81 \rightarrow 17,81 \rightarrow 110,81 \rightarrow 101,81 \rightarrow 127, \\
& \cdots 18159 \rightarrow, 75 \rightarrow 96,75 \rightarrow 23,75 \rightarrow 3,75 \rightarrow 117,75 \rightarrow 164,75 \rightarrow 48,75 \rightarrow 267, \\
75 & \rightarrow 61,75 \rightarrow 81,75 \rightarrow 35,75 \rightarrow 41,75 \rightarrow 16,75 \rightarrow 50,75 \rightarrow 19,75 \rightarrow 27,75 \rightarrow 104, \\
75 & \rightarrow 31,75 \rightarrow 25,75 \rightarrow 142,75 \rightarrow 80,75 \rightarrow 145,75 \rightarrow 54,75 \rightarrow 20,75 \rightarrow 98, \\
75 & \rightarrow 1,75 \rightarrow 91,75 \rightarrow 85,75 \rightarrow 21,75 \rightarrow 5,75 \rightarrow 163,75 \rightarrow 89,75 \rightarrow 53,75 \rightarrow 238, \\
75 & \rightarrow 55,75 \rightarrow 427,75 \rightarrow 114,75 \rightarrow 30,75 \rightarrow 58,75 \rightarrow 497,75 \rightarrow 51,75 \rightarrow 105\}
\end{aligned}
$$

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To get the weights, we can just take the first element. Easy!
ln[6]:= weights = First/@ links

$$
\begin{aligned}
& \{42,92,148,203,28,38,48,491,52,207,67,56,112,76,129,139,46,66,66,82, \\
& 76,41,32,43,35,7,32,43,93,95,61,47,105,42,119,28,16,37,23,54, \\
& 23,27,78,79,114,75,112,156,12,115,119,47,26,60,33,22,35,87,16, \\
& 63,115,34,111,44,57,56,37,47,111,17,85,104,22,46,70,47,36,34, \\
& 18,23,82,20,24,47,25,57,17,41,20,15,21,50,90,15,97,41,16,125, \\
& 30,42,34,15,32, \ldots 18036 \cdots, 1,2,1,2,4,1,1,4,2,1,1,1,1,1,1,1,1 \text {, } \\
& 1,1,1,2,1,2,2,1,1,1,1,2,1,1,1,1,1,1,1,4,2,1,1,3,3,2,2,2,1 \text {, } \\
& 1,2,1,1,4,1,1,2,1,1,2,1,4,3,8,2,2,1,1,2,3,2,1,1,2,1,2,1,1, \\
& 1,3,2,1,2,2,2,3,1,1,2,1,1,1,1,1,1,1,2,1,1,1,1,1,1,2,1,1\}
\end{aligned}
$$

| large output | show less | show more | show all | set size limit... |
| :--- | :--- | :--- | :--- | :--- |

Excellent! We are now ready to plot our graph..... or.... are we? See how there are more than 18 K edges. Ouch. I hope this doesn't break my laptop.
$\ln [7]:=$ biggraph $=$ Graph[edges, EdgeWeight $\rightarrow$ weights]


Gross. Well, it doesn't really look like anything so it's difficult to get any information out of looking at it. Instead, it would be much easier to apply some measures to gain a sense of what is happening!

## Let's blast it with measures!

In the documentation, you can search "graph properties and measurements" and a whole bunch of things will pop up.
ln[8]:= VertexCount [biggraph]
EdgeCount[biggraph]

Out[8]= 141
Outipl= 18242

## $\ln [22]:=$

## VertexDegree[biggraph]

## VertexList[biggraph]

SortBy[Transpose[\{VertexList[biggraph], VertexDegree[biggraph]\}], Last]
Out 22$]=\{280,274,279,280,280,266,265,273,280,273,280,276,274,279,276,279$, 280, 267, 275, 277, 278, 276, 263, 268, 266, 260, 219, 274, 267, 280, 277, 279, 267, 278, 274, 278, 263, 230, 266, 259, 265, 254, 246, 280, 273, 279, 276, 279, $280,221,279,280,274,242,270,254,248,261,278,247,275,278,253,280$, $278,275,278,267,273,278,246,280,280,250,279,275,274,264,263,260$, $249,278,268,258,272,260,272,230,276,268,262,249,274,280,219,279$, 267, 239, 279, 263, 276, 258, 245, 260, 249, 250, 274, 276, 275, 268, 277, $216,203,271,247,237,266,256,233,241,223,223,243,273,243,266$, 259, 258, 211, 231, 167, 246, 202, 256, 166, 224, 158, 220, 240, 144, 184\}

Out [23]= $\{81,53,43,164,145,240,99,62,236,432,555,238,28,202,516,8,104$, $31,114,41,64,201,51,1,96,79,83,98,13,40,107,85,203,58,245$, $5,35,26,136,17,110,101,127,7,80,119,16,25,157,222,27,39,50$, $38,126,19,111,29,4,2,56,117,131,267,77,23,91,92,141,497,6$, $142,24,161,9,121,54,34,421,3,45,63,69,59,143,90,21,113,55$, $82,44,103,498,12,60,163,112,254,48,67,105,89,84,20,22,133$, $266,76,412,11,122,154,429,78,72,74,37,134,18,268,42,150,115$, $36,30,68,61,15,420,14,32,86,57,10,33,427,102,120,223,75,106\}$

Out[24] $=\{\{75,144\},\{102,158\},\{33,166\},\{32,167\},\{106,184\},\{57,202\},\{429,203\}$, $\{420,211\},\{154,216\},\{60,219\},\{83,219\},\{120,220\},\{222,221\},\{42,223\}$, $\{150,223\},\{427,224\},\{26,230\},\{113,230\},\{14,231\},\{18,233\},\{74,237\}$, $\{254,239\},\{223,240\},\{268,241\},\{38,242\},\{30,243\},\{115,243\},\{84,245\}$, $\{6,246\},\{86,246\},\{127,246\},\{2,247\},\{72,247\},\{111,248\},\{22,249\}$, $\{45,249\},\{103,249\},\{133,250\},\{161,250\},\{131,253\},\{19,254\},\{101,254\}$, $\{10,256\},\{134,256\},\{15,258\},\{59,258\},\{89,258\},\{17,259\},\{61,259\}$, $\{3,260\},\{20,260\},\{79,260\},\{90,260\},\{29,261\},\{44,262\},\{35,263\},\{51,263\}$, $\{67,263\},\{421,263\},\{34,264\},\{99,265\},\{110,265\},\{37,266\},\{68,266\}$, $\{96,266\},\{136,266\},\{240,266\},\{13,267\},\{31,267\},\{92,267\},\{112,267\}$, $\{203,267\},\{1,268\},\{11,268\},\{69,268\},\{82,268\},\{126,270\},\{78,271\}$, $\{21,272\},\{143,272\},\{36,273\},\{62,273\},\{80,273\},\{141,273\},\{432,273\}$, $\{28,274\},\{50,274\},\{53,274\},\{54,274\},\{98,274\},\{245,274\},\{266,274\}$, $\{498,274\},\{23,275\},\{56,275\},\{114,275\},\{121,275\},\{412,275\},\{16,276\}$, $\{55,276\},\{76,276\},\{105,276\},\{201,276\},\{238,276\},\{516,276\},\{41,277\}$, $\{107,277\},\{122,277\},\{4,278\},\{5,278\},\{58,278\},\{63,278\},\{64,278\}$, $\{77,278\},\{91,278\},\{117,278\},\{497,278\},\{8,279\},\{9,279\},\{25,279\}$, $\{27,279\},\{43,279\},\{48,279\},\{85,279\},\{119,279\},\{163,279\},\{202,279\}$, $\{7,280\},\{12,280\},\{24,280\},\{39,280\},\{40,280\},\{81,280\},\{104,280\}$, $\{142,280\},\{145,280\},\{157,280\},\{164,280\},\{236,280\},\{267,280\},\{555,280\}\}$

So many things we could explore, so let's focus on a game-centric aspect.
Since A-->B means that character A beat character B, character A would be really a really good charac-
ter to play if it a ton of out-degrees and very little in-degrees! Let's explore this idea a little bit. First, what is the distribution of all degrees? In degree and out degrees together? Separate?
$\ln [43]:=$ ListPlot[VertexDegree[biggraph] // Sort, PlotLabel $\rightarrow$ "Degree Distribution, Sorted"]


The x-axis doesn't matter here since the numbers are just labels for characters.
In[30]:= ListPlot[VertexInDegree[biggraph] // Sort, PlotLabel $\rightarrow$ "In-Degree Distribution, Sorted"]


```
ListPlot[VertexOutDegree[biggraph] // Sort,
    PlotLabel }->\mathrm{ "Out-Degree Distribution, Sorted"]
```

Out-Degree Distribution, Sorted


It looks like, for the most part, the majority of characters have similar in-degree and out-degree, except for a small handful of characters. Perhaps these characters are unpopular or something. Let's see the ratio of out-degree and in-degree. A high ratio indicates a character beats more characters than loses against more characters.

In[44]: $=$ ListPlot[(VertexOutDegree[biggraph] /VertexInDegree[biggraph]) // Sort, PlotLabel $\rightarrow$ "Out/In Degree Distribution, Sorted"]

Out/In Degree Distribution, Sorted


Whoa! That looks really cool! Those characters on the right must be really good, and the ones on the left must be really bad...
However, it may not be actually be reflective of our intuition since there are edge weights. Some edges are really heavy, meaning there may A-->B for a TON of matches and B-->A for only one or two matches. The edges are not equal! Let's see if there are measures that take edge weight into account. Also A-->B edges and $\mathrm{A}-\mathrm{-} \mathrm{C}$ edges can have different weights too.

Back to the guide!

EigenvectorCentrality is a really good one to use. It's a lot like Page Rank. Basically, it means that if someone is connected a LOT to a bunch of other people, it has a higher value. But it has an even HIGHER value if all the nodes are connected to have a high value! Intuitively, it means you're more popular if you have lots of popular friends.

In[38]:= ListPlot[EigenvectorCentrality[biggraph, "In"] // Sort, PlotLabel $\rightarrow$ "EVC (In-degrees), Sorted"]

EVC (In-degrees), Sorted


In[39]:= ListPlot[EigenvectorCentrality[biggraph, "Out"] // Sort, PlotLabel $\rightarrow$ "EVC (Out-degrees), Sorted"]

EVC (Out-degrees), Sorted


```
\(\ln [41]:=\) ListPlot[
(EigenvectorCentrality[biggraph, "Out"] /EigenvectorCentrality[biggraph, "In"]) //
Sort, PlotLabel \(\rightarrow\) "EVC (Out/In degrees), Sorted"]
```



Most excellent! Now we can, with a higher degree of confidence, say that these make intuitive sense.

